Assignment 6

Byungjoon Min, Quantum Mechanics II (due date: November 5, 2018)

1 Angular Momentum [30 pt]

Show that the spherical harmonics are eigenfunctions of L^2 and L_z . To be specific, derive Eq. [4.132] from Eq. [4.123]. If you want to use an alternative way instead of Griffiths', any methods are welcome.

2 Energy of a magnetic dipole [20 pt]

Consider a magnetic dipole m being in a magnetic field B. Show that the energy of a magnetic dipole in the field is given by

$$U = -m \cdot B. \tag{1}$$

Also, show that the force to this dipole is

$$F = -\nabla(-m \cdot B). \tag{2}$$

See Chap. 6 of Introduction to Electodynamics, D. J. Griffiths.